

# Implementation of machine learning techniques to predict impact parameter and transverse sphericity in heavy-ion collisions at the LHC

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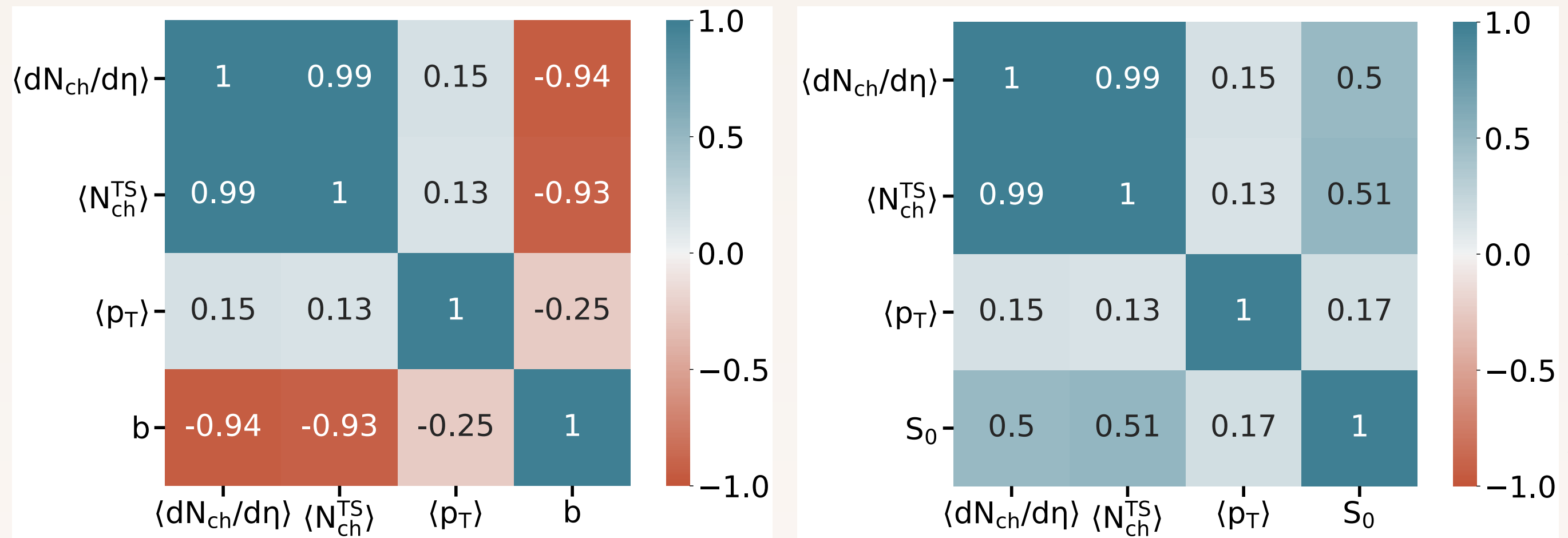
Based on [Phys. Rev. D 103, 094031 \(2021\)](#)

## 1. Introduction

- Machine learning is being used in various **classification and regression** problems
- ML gives ability to the machine to **predict an outcome without being explicitly programmed**
- A multi-phase transport (AMPT) model is used for data generation
- **Impact parameter** is a crucial observable in heavy-ion collisions yet almost **impossible to predict** in experiments
- **Transverse sphericity**, an event shape observable, has recently been introduced in heavy-ion collisions to **study azimuthal anisotropy** [1]
- In the absence of any experimental exploration, **ML could be used to estimate sphericity**

1. N. Mallick, R. Sahoo, S. Tripathy, and A. Ortiz, [J. Phys. G 48, 045104 \(2021\)](#)

## 2. Observables

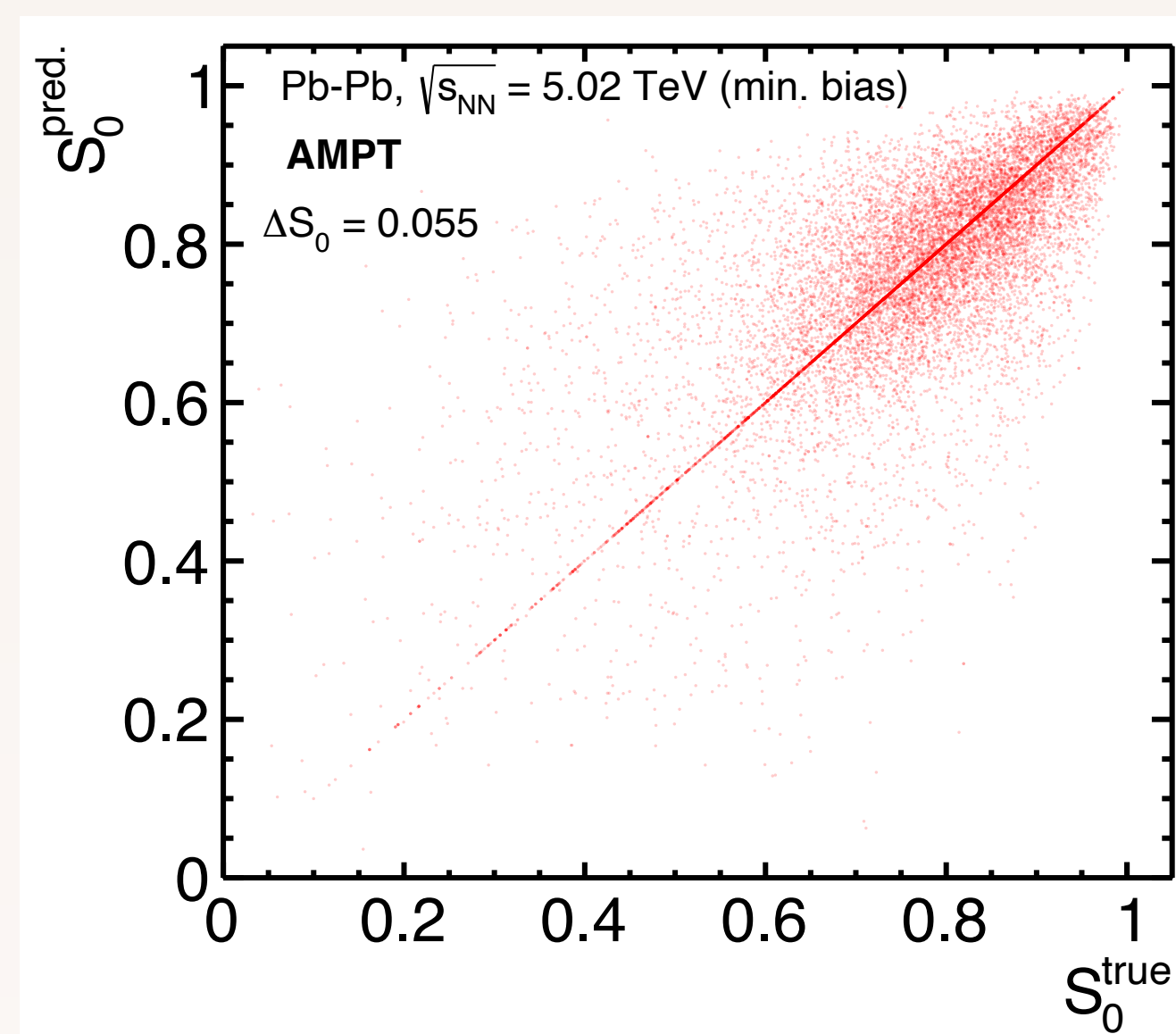
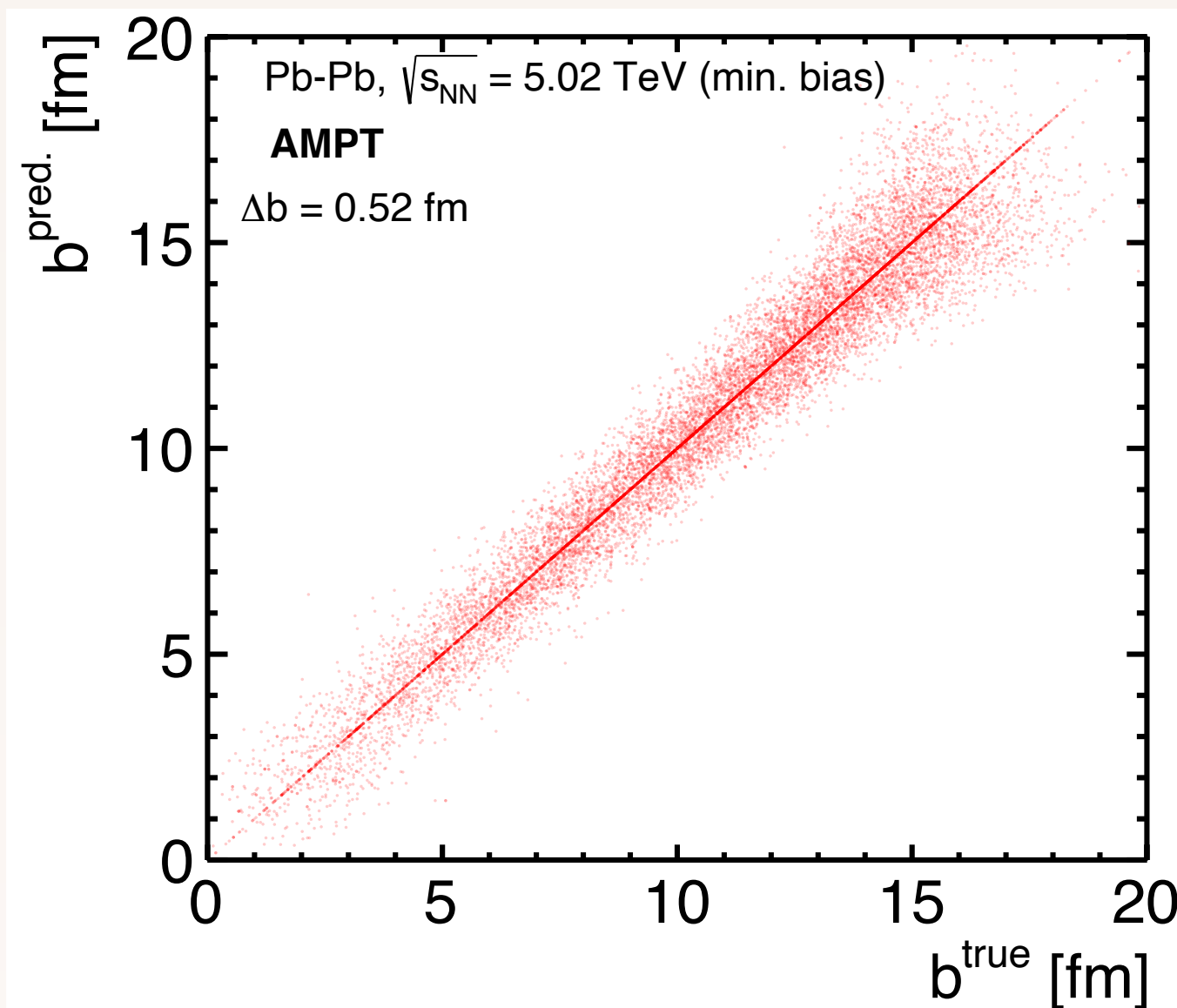
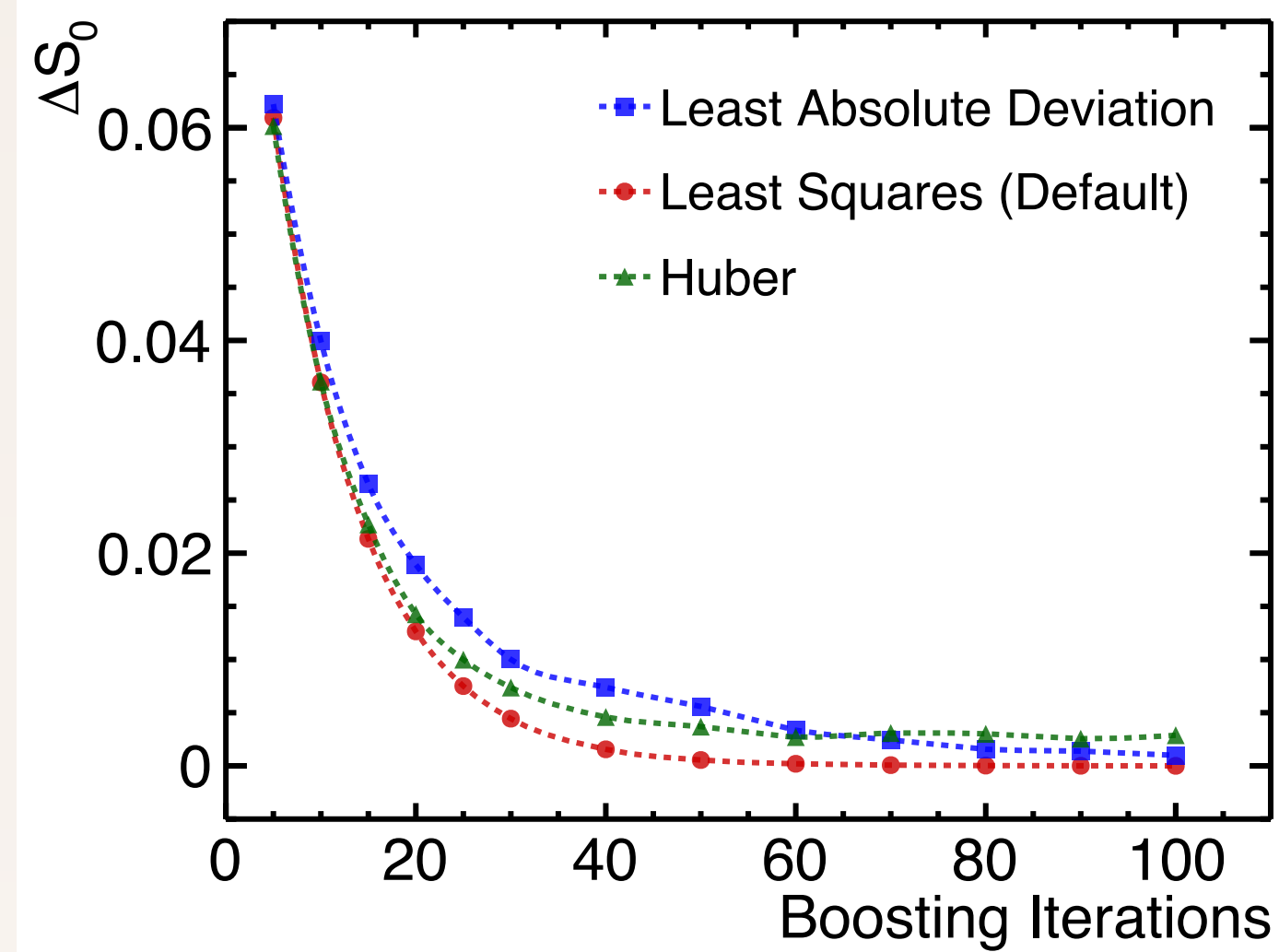
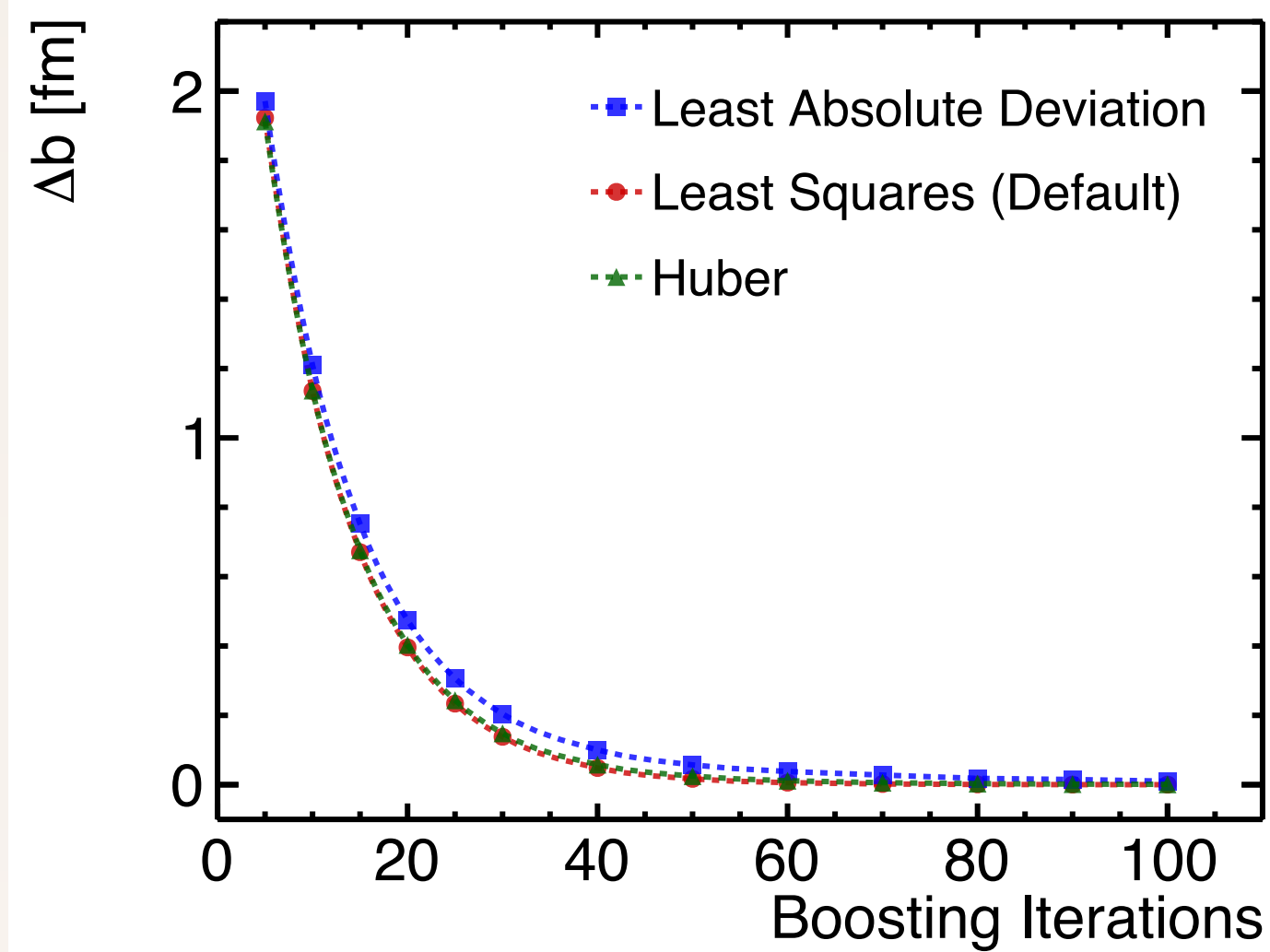


- Final state observables such as **charged particle multiplicity, charged particle multiplicity in the transverse region and mean transverse momentum** are chosen as the input
- Pearson correlation coefficient indicates **strong linear correlation** among the chosen input and target observables

## 2. Method

- **Gradient boosting decision trees (GBDTs)** for regression [2,3]
- Loss function: **Least squares**, **Least absolute deviation** and **Huber function**
- Maximum number of trees: 100
- Learning rate: 0.1, Maximum depth: 40
- Training sample size: 60,000 events
- The **least difference in  $\Delta b$  and  $\Delta S_0$**  among the different loss functions are taken as the **systematic uncertainty**

$$\Delta b = \frac{1}{N_{\text{events}}} \sum_{n=1}^{N_{\text{events}}} |b_n^{\text{true}} - b_n^{\text{pred.}}|$$



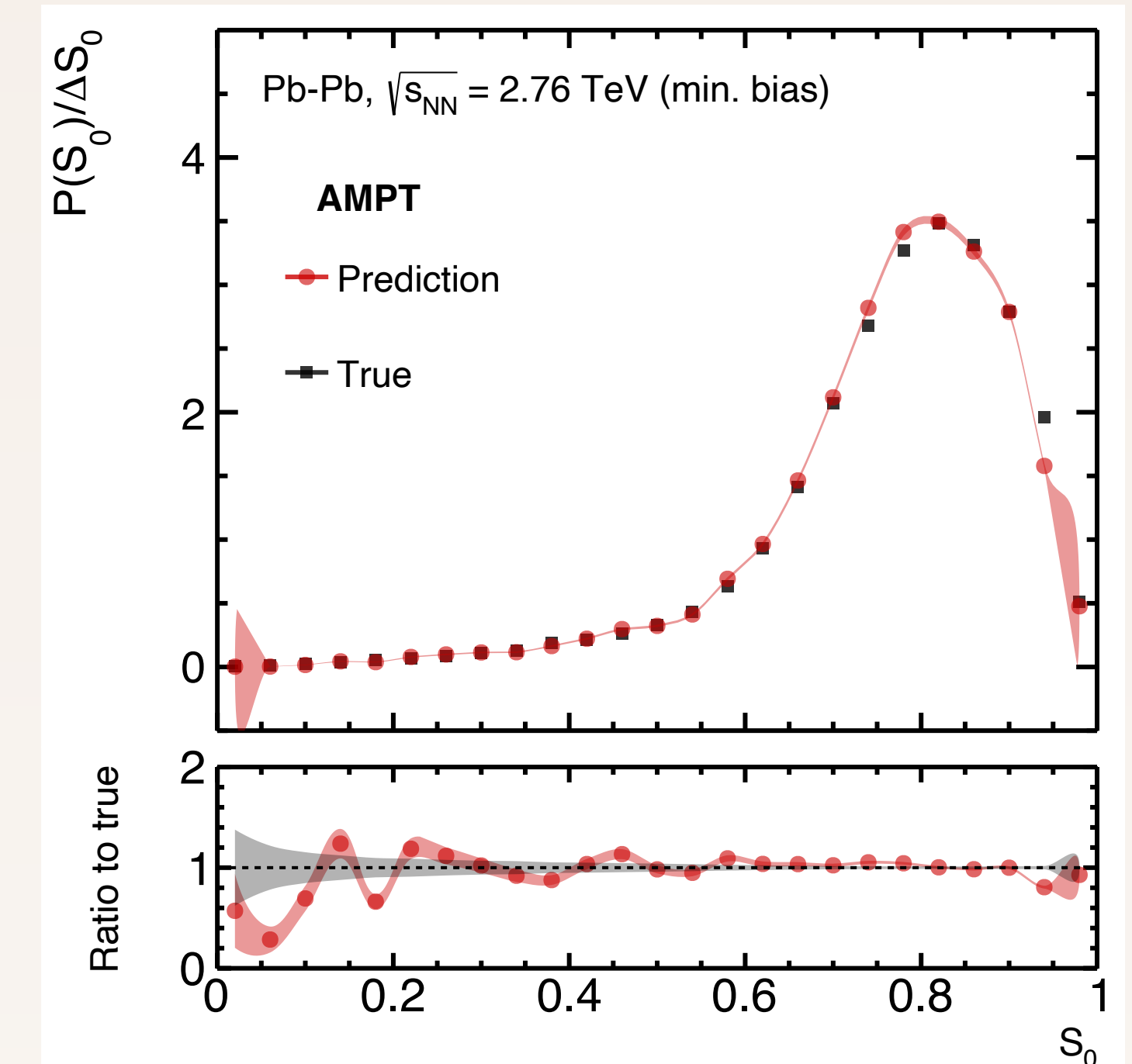
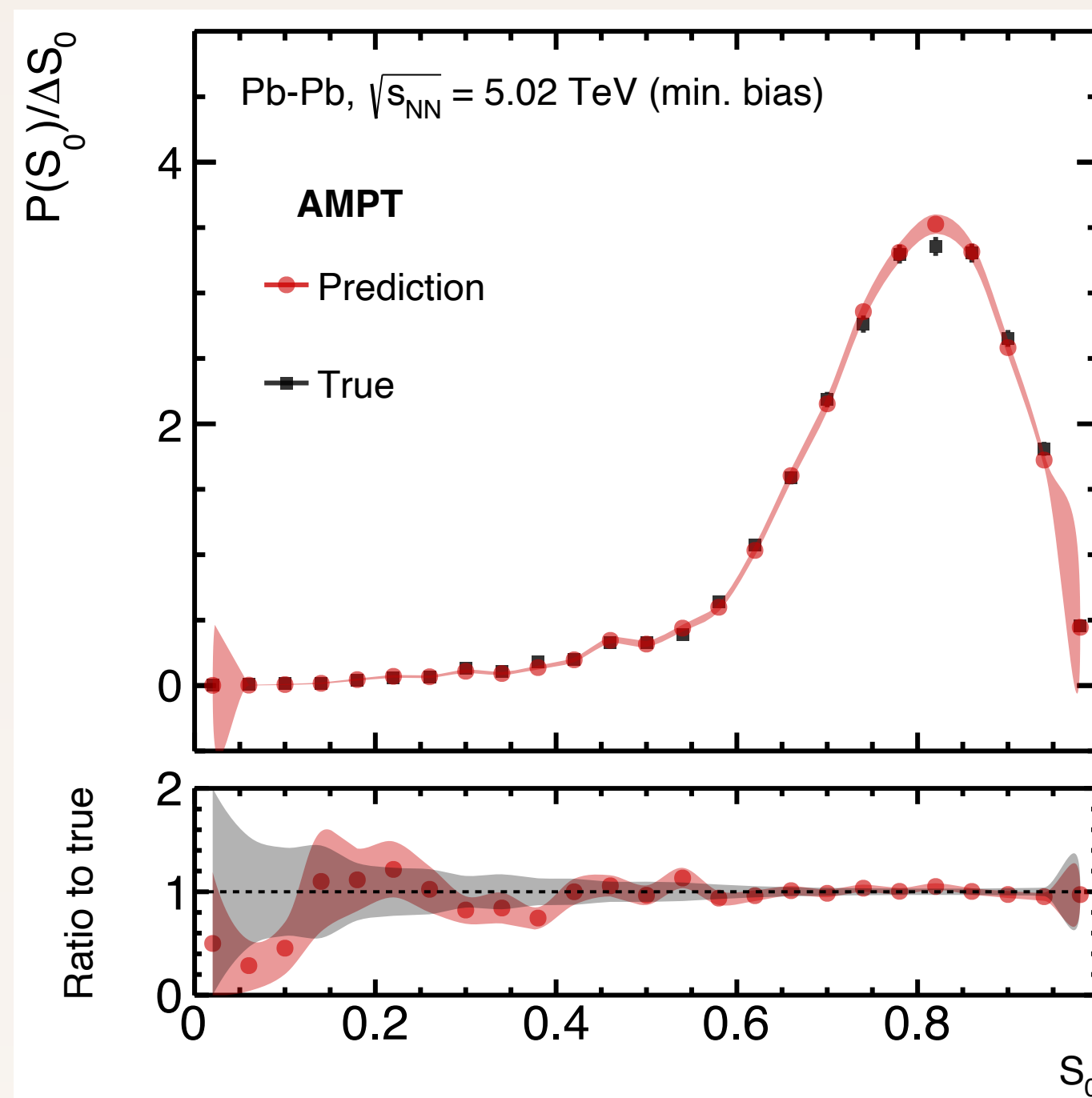
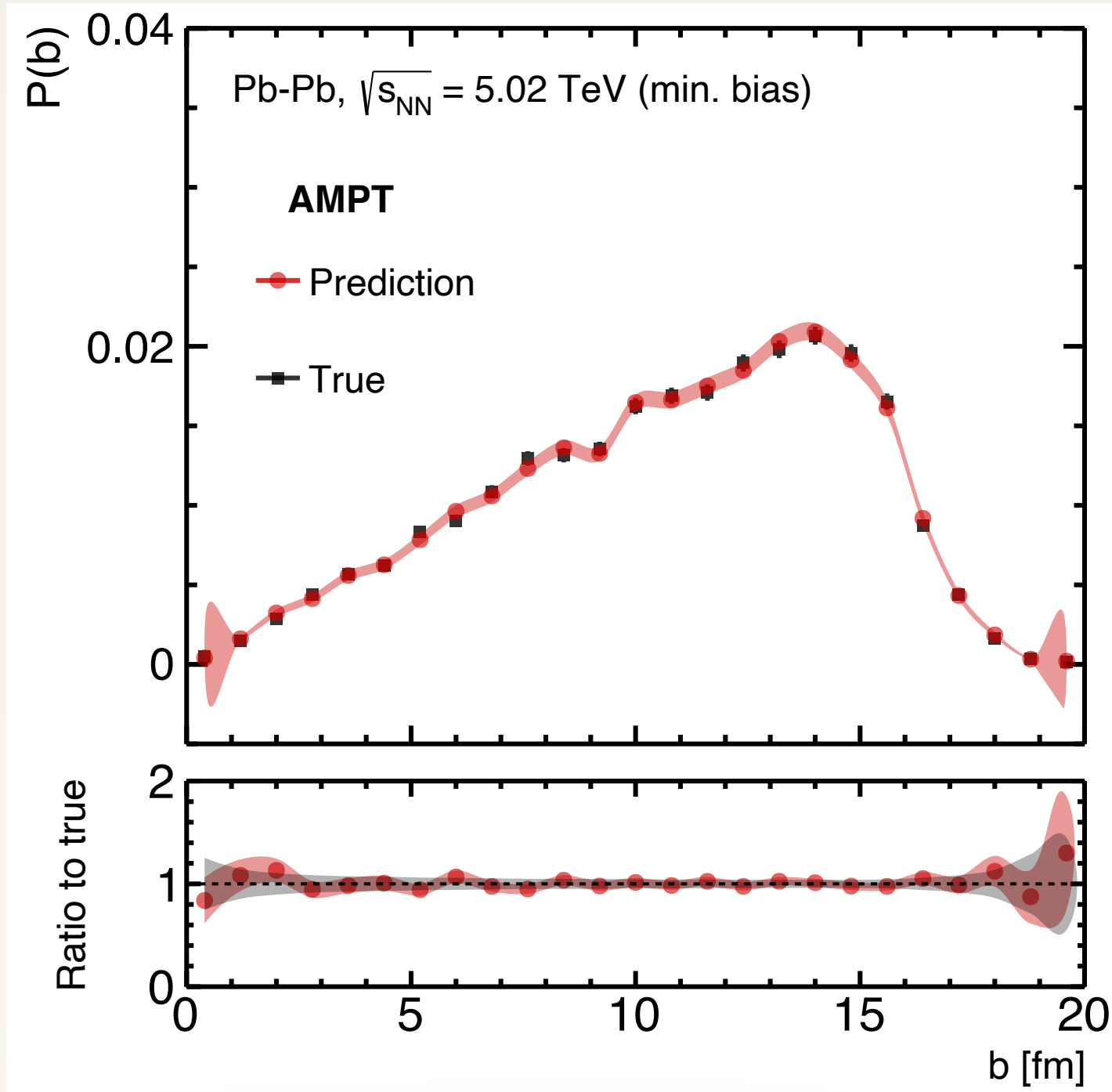
Size of training data	2K	10K	20K	40K	50K	60K
$\Delta b$ [fm]	0.71	0.62	0.58	0.53	0.52	0.52
$\Delta S_0$	0.079	0.068	0.062	0.058	0.056	0.055

- **Least squares loss function** gives minimum  $\Delta b$  and  $\Delta S_0$
- Training error **saturates at 60K events**
- Prediction error for  **$\Delta b = 0.52$  fm** and  **$\Delta S_0 = 0.055$**
- Prediction vs. true plot shows **a straight line with slope = 1**

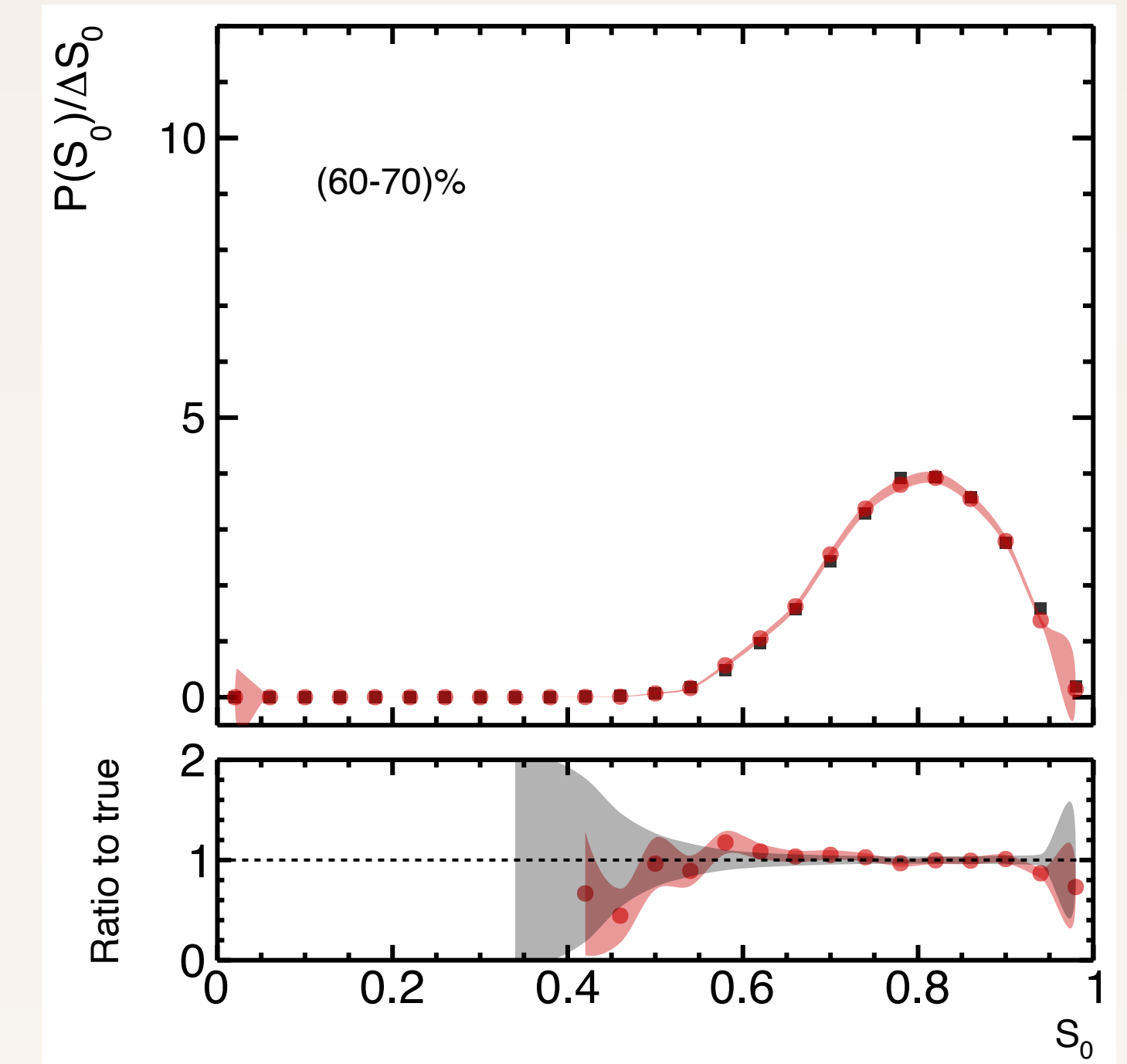
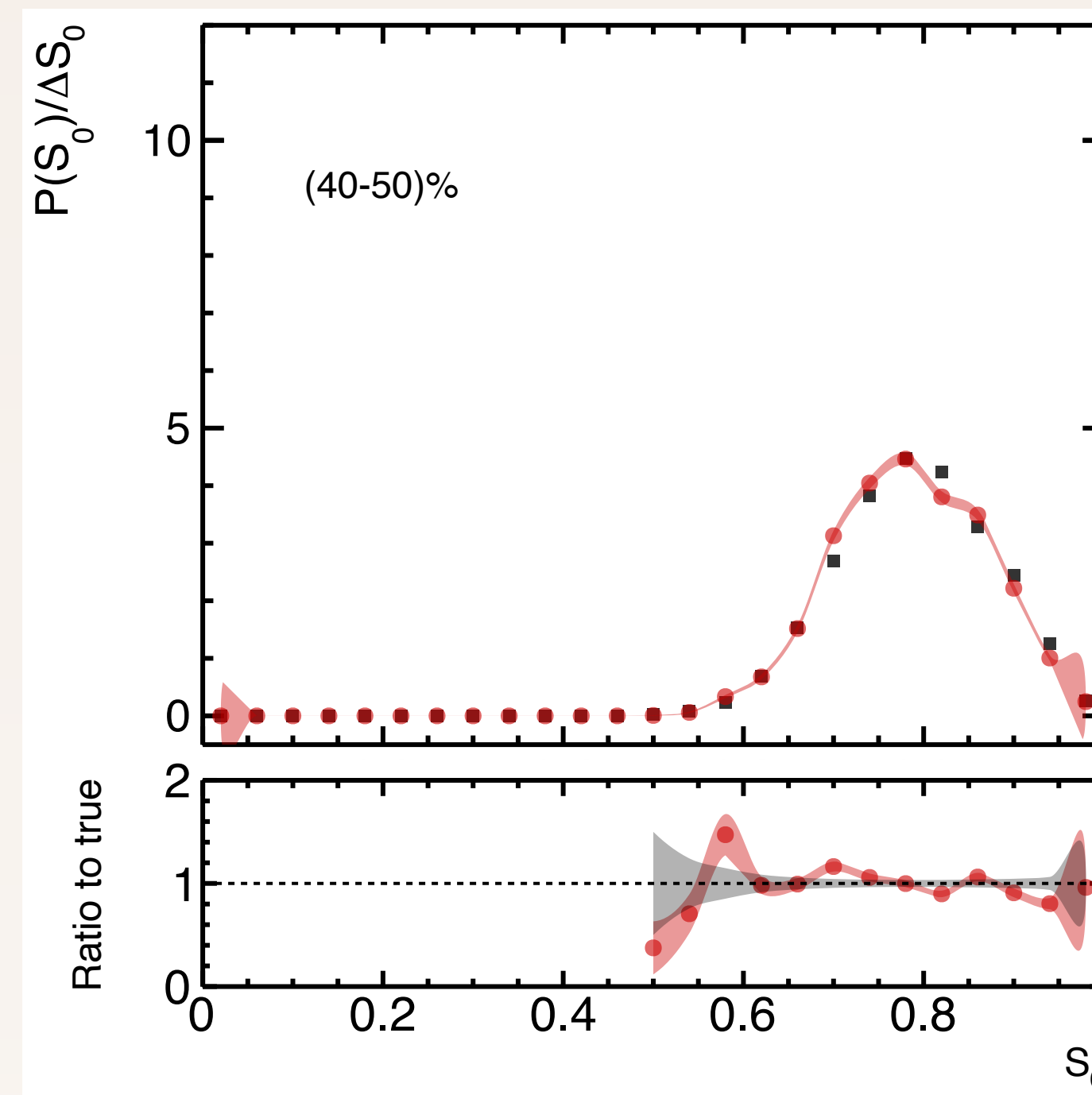
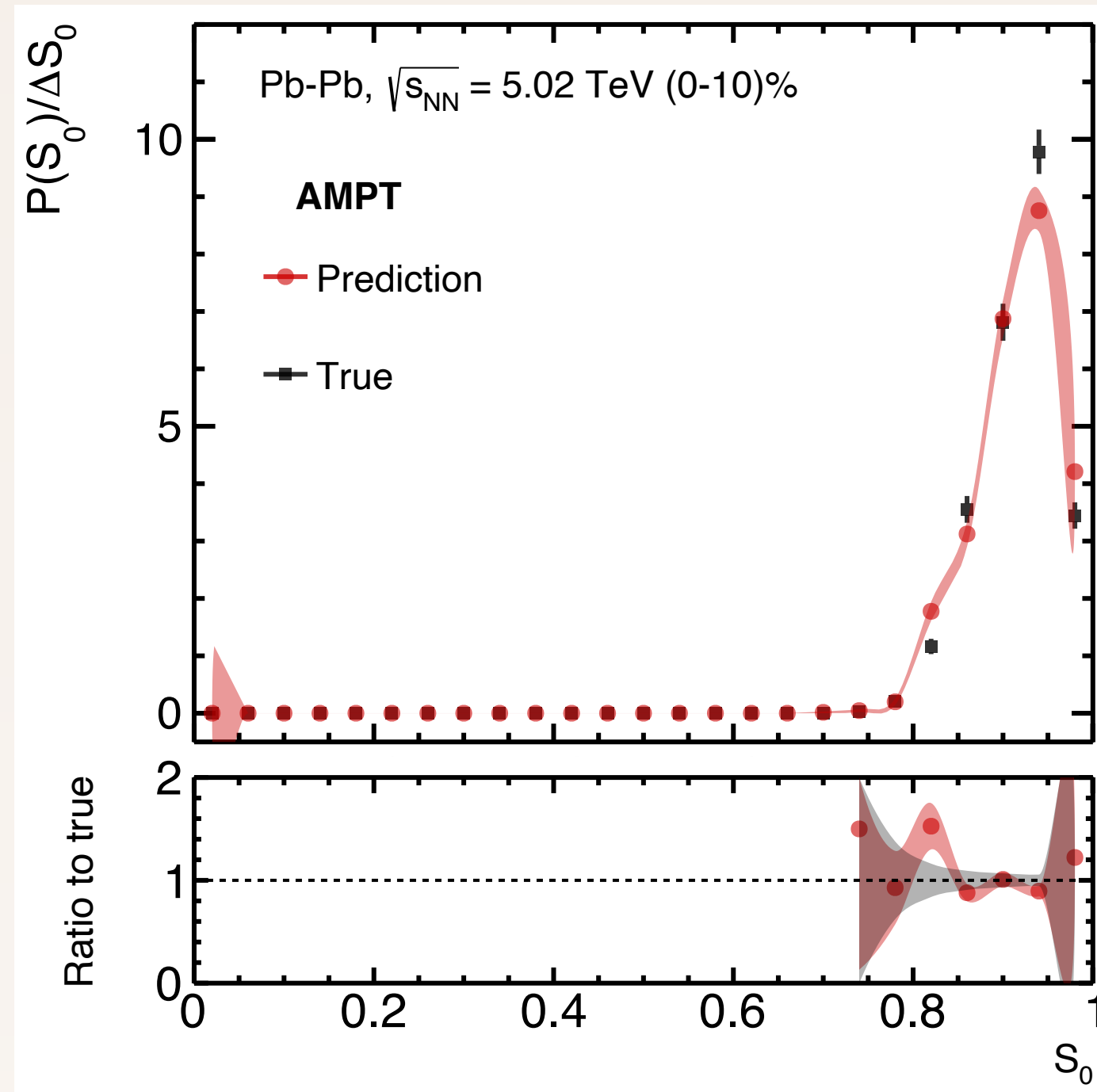
2. J. H. Friedman, [Ann. Stat. 29, 1189 \(2001\)](#).

3. L. Breiman, J. H. Friedman, R. A. Olshen, and C. J. Stone, *Classification and Regression Trees* (Wadsworth & Brooks/ Cole Advanced Books & Software, Monterey, CA, 1984), p. 358, <https://doi.org/10.1002/cyto.990080516>.

### 3. Results and discussions



- Training for impact parameter and transverse sphericity is done on Pb-Pb collisions,  $\sqrt{s_{\text{NN}}} = 5.02$  TeV (min. bias) data from AMPT
- Black band denotes **statistical uncertainty** in simulated (true) values
- Red band denotes the **quadratic sum of statistical and systematic uncertainty** in the predicted values from the ML-model
- The predictions for impact parameter and transverse sphericity in Pb-Pb collisions,  $\sqrt{s_{\text{NN}}} = 5.02$  TeV (min. bias) are in **good agreement with the true values**
- ML-model trained on Pb-Pb collisions,  $\sqrt{s_{\text{NN}}} = 5.02$  TeV (min. bias) data **successfully predicts** transverse sphericity distribution for Pb-Pb collisions,  $\sqrt{s_{\text{NN}}} = 2.76$  TeV (min. bias)



- Training for transverse spherocity is done on **Pb-Pb collisions,  $\sqrt{s_{NN}} = 5.02$  TeV (min. bias)** data from AMPT
- Black band denotes **statistical uncertainty** in simulated (true) values
- Red band denotes the **quadratic sum of statistical and systematic uncertainty** in the predicted values from the ML-model
- ML-model trained on **Pb-Pb collisions,  $\sqrt{s_{NN}} = 5.02$  TeV (min. bias)** data **successfully predicts** the transverse spherocity distributions at various centralities such as (0-10)%, (40-50)% and (60-70)%